

## CHANCE CONSTRAINED PROGRAMMING (CCP) WITH INDEPENDENT OR DEPENDENT EXPONENTIAL INPUT COEFFICIENTS

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### ABSTRACT

In this paper, we consider Chance constrained programming (CCP) technique when at least two of the LHS input coefficients are random and distributed as two-parameter exponential distribution- Since two-parameter exponential distribution is more applicable in most real life applications than the single-parameter exponential distribution.

Two approaches are introduced to transform CCP into deterministic: (i) The first approach proposed under the assumption of independence between exponential variables and (ii) the second approach assumes that random input coefficients are dependent with correlation coefficient  $\rho$ .

The first approach of independence is an extension of Biswal's approach to deal with two-parameter exponential variables instead of single-parameter exponential variables. That is through two lemmas and a theorem for  $m$  independent input coefficients. The second approach of dependence uses Downton bivariate exponential distribution for reflecting the joint distribution of correlated input coefficients under two cases; the first introduced case assumes that dependent input coefficients have single-parameter exponential marginals and the second introduced case is an extension of Downton bivariate exponential distribution for case of two-parameter exponential random input coefficients. The deterministic equivalent of chance constraints are obtained through a theorem and a corollary for each case.

Finally; It was shown that the equivalent deterministic transformation for the extension of Downton exponential distribution for two-parameter exponential marginals is a generalization of the first approach for  $m=2$  when the correlation coefficient is zero and the second approach for single-parameter exponential marginal when the second parameter is zero.

**Keywords:** *Bessel function, Biswal approach, chance constrained programming, Downton bivariate exponential distribution, input coefficients, Non-linear programming, two-parameter exponential distribution.*

### 1. INTRODUCTION

In the nineteenth